

RYERSON UNIVERSITY
MTH 714 LAB#11
DAY: NOVEMBER 20, 2008

1. Which of the following sets of clauses are satisfiable?

(a) $\{\neg p(x, y) \vee \neg p(y, x), p(f(x), f(x))\}$

(b) $\{\neg p(x, y) \vee \neg p(y, x), p(f(f(x)), f(y))\}$

(c) $\{\neg p(x, y) \vee \neg p(y, z) \vee p(x, z), \neg p(f(x), f(f(f(x))))\}, p(x, f(x))\}$

2. Exercise 10 from 7.9.

3. Is the formula

$$\forall x \exists y \forall z [p(f(x), y) \vee p(y, f(z))]$$

a logical consequence of the set of formulas

$$\{\forall x \exists y [p(x, f(y)) \rightarrow p(y, f(x))], \exists x \forall y \exists z [\neg p(x, f(y)) \rightarrow \neg p(y, f(z))]\}$$